

Hint for the problem about Wiener filter

Signal model :

$$s(x, y) = \hat{s}(x, y) + n(x, y), \quad (1)$$

where $s(x, y)$ is observed signal with noise.

Filtered spectrum by Wiener filter:

$$\tilde{\mathcal{S}}(k_x, k_y) = \Phi(k_x, k_y) \mathcal{S}(k_x, k_y), \quad (2)$$

$$\Phi(k_x, k_y) = \frac{|\mathcal{S}(k_x, k_y)|^2 - |\mathcal{N}'(k_x, k_y)|^2}{|\mathcal{S}(k_x, k_y)|^2}, \quad (\Phi \geq 0). \quad (3)$$

Since the noise is a white noise in this problem, the noise spectrum is flat. From this nature, we can estimate $|\mathcal{N}'|^2$ from $|\mathcal{S}(k_x, k_y)|$ in the spectral domain where the signal is not significant.

Procedure

1. Compute Fourier transform, $\mathcal{S}(k_x, k_y)$, of the original image, $s(x, y)$.
2. Determine the domain where the signal is not significant (noise dominant domain) by seeing $|\mathcal{S}(k_x, k_y)|$.
3. Determine the noise level from noise dominant domain. It can be considered as a constant.
4. Compute Wiener Filter $\Phi(k_x, k_y)$.

Since $\Phi \geq 0$, if the numerator of Φ has a negative value, it should be truncated to 0.
For the periodic noise, Φ at the frequency of the periodic noise can be also truncated to 0.

5. Compute filtered spectrum $\tilde{\mathcal{S}}(k_x, k_y)$.
6. Compute filtered image $\tilde{s}(x, y)$ by applying inverse Fourier transform.